



Pattern Formation and Adaptation in Multi-Robot Systems

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Abstract

The ability to deploy huge numbers of low-cost robots for duties like surveillance and search has just become viable because to advancements in robotics. It is still difficult to solve the challenge of coordinating several robots to do such duties. Recent research papers on multi-robot systems are summarized in this report. It's divided into two sections. In the first section, we discussed research into the pattern formation challenge, or how to guide a team of robots to and through a coordinated configuration. The second section summarizes the research on multi-robot system control that made use of adaptive techniques. We have looked at (1) the use of learning (perpetual adaptation) to make multi-robot systems adjust to environmental and individual robot capability changes, and (2) the use of evolution to develop group behaviors.

Introduction

The ability to deploy huge numbers of low-cost robots for duties like surveillance and search has just become viable because to advancements in robotics. However, coordinating a group of robots to carry out such jobs is still difficult to do. Previous studies on multi-robot systems have taken a more generalized approach (see, for example, the works of Cao et al.[25] and Dudek et al.[7]). In contrast to these, the focus of this article is confined to the most up-to-date research on pattern creation and adaptability in multi-robot systems. The report has two sections. Part one

of this series examined research into the pattern formation challenge, or how to command a swarm of robots to build and hold a certain pattern. The second section discusses the research done on multi-robot systems that employed adaptation techniques for command. Our research has focused on (1) the use of learning (continuous adaptation) to enable multi-robot systems to react to variations in both the environment and the capabilities of individual robots, and (2) the application of evolution to the generation of collective behaviors.

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Pattern formation in multi-robot systems

Coordinating a collection of robots into and keeping them in a predetermined arrangement (such a wedge or a chain) is the pattern formation challenge. Search-and-rescue operations, landmine disposal, remote terrain and space research, satellite array management, and unmanned aerial vehicles (UAVs) are only few of the current areas of use for pattern creation. Cooperative actions among members of different animal species have also been shown to result in pattern creation. In these cases, animals either maintain a consistent orientation and distance from one another while on the move or cover an area with as much uniformity as feasible. Animals often develop patterns, and bird flocks, fish schools, and ant chains are just a few examples [18].

We divide the research on pattern creation into two categories. The first set of investigations include a centralized unit that manages the team and issues orders to each robot individually. Methods for forming distributed patterns to achieve coordination compose the second category.

Centralized pattern formation

A computational unit monitors the whole group and arranges the members' movements appropriately in centralized pattern creation methods [3, 13, 23, 24]. Each robot's motion is then sent to it through some kind of network. Coordinated movement of many robots along a predetermined route is proposed by Egerstedt and Hu [13]. Separation between route planning and tracking is achieved. It's centralized, and the monitoring of fictitious landmarks is performed independently. The robots are directed by a virtual leader whose course is calculated in advance. They used it to get a group of virtual robots to navigate around a triangle of obstacles. The robots in this case formed a triangle, and its corners navigated around an obstruction that had been placed in their path. The research demonstrates that the provided strategy stabilizes the formation error if the robots' tracking mistakes are constrained or tracking is done precisely. To get a flock of UAVs to fly in formation, Koo and Shahruz [23] suggest using a centralized path-planning technique. One, more competent UAV determines the course for the others to follow. Cameras and sensors are only available to the leader. Through a communication connection, it

instructs the other UAVs on the paths they should be following. It is recommended that UAVs launch themselves in the direction of their trajectories and then latch onto them. Experiments investigate both a scenario in which UAVs take off one by one and another in which they all take off at once. The study's primary emphasis is trajectory computation. Belta and Kumar [3] provide a kinetic energy shaping centralized trajectory calculation system. They use a gradually varying kinetic energy meter rather than a constant one. The procedure provides smooth paths for a group of mobile robots to follow. Using a parameter, you may adjust how close the robots are to one another. However, the strategy is not scalable since it does not account for avoiding obstacles. Kowalczyk [24] details a target assignment technique for the formation building issue. In order to achieve the required configuration out of a dispersed collection of robots, the algorithm must first give each robot a target point. Then it creates the priorities and paths the robots need to follow to go where they're going without colliding with each other. There is a buffer zone surrounding each robot's route where robots with lesser priority aren't allowed to go. The robot will wait for the higher priority robot to move out of the way if its path takes it through an area that is off limits to it. Both holonomic and non-holonomic robots are used to validate the approach. The technique presupposes the availability of a centralized processing power and global sensing capability. The method's potential for expansion evades the question. Strategies for centralized pattern creation presume the presence of a communication connection between the central unit and the individual robots, and depend on a single node to manage the whole group. Because of these presumptions, the centralized approach is more difficult to implement, less able to recover from errors, and less competent to manage a large fleet of robots. Decentralized pattern creation techniques provide an option.

Decentralized pattern formation

Communication and completeness of information known by robots impose a trade-off between precision and feasibility of forming and maintaining the pattern and the necessity of global information and

communication. Studies that require global information or broadcast communication [29, 19, 12] may suffer from lack of scalability or high costs of the physical setup but allow more accurate forming of a greater range of formations.

On the other hand, studies using only local communication and sensor data [21, 22, 10, 5, 17, 15, 9, 11] tend to be more scalable, more robust, and easier to build; but they are also limited in variety and precision of formations. Sugihara and Suzuki [12] achieved pattern formation by providing each robot the global positions of all others. In this study, an algorithm is developed for each pattern. The proposed method can uniformly distribute robots creating different pattern formations (circles, polygons, line, filled circle, and filled polygon). It can also split a group of robots into an arbitrary number of nearly equal sized groups. Despite the impressive results obtained by this decentralized algorithm, the global communication required to share information among the whole group, makes it less scalable. Carpin and Parker [19] introduced a cooperative leader following strategy for a team of robots. The robots are able to maintain a specific formation while simultaneously moving in a linear pattern and avoiding dynamic obstacles. The robots use local sensor information and explicit broadcast communication among themselves. The framework handles heterogeneous teams, i.e. comprising of robots with different types of sensors, as well as homogeneous ones.

Two levels of behaviors were implemented for tasks: team-level and robot-level behaviors. Transitions are made when necessary among specific behaviors in these two levels. For example, when a member of the team faces an obstacle, the whole team waits together with that member for it to go away for a certain amount of time. If this time is exceeded that member circumnavigates the obstacle and the team returns to its main task of moving in a formation. Balch and Hybinette [21, 22] proposed a different strategy for robot formation that is inspired from the way molecules form crystals. In this study, each robot has several local *attachment sites* that other robots may be attracted to. This concept is similar to molecular covalent bonding. Possible attachment site geometries include shapes resembling where the robot is the center of the shape and the attachment sites are the ends of the line segments. Various robot formation shapes result from usage of different attachment site geometries just as different crystal shapes emerge from various covalent bond geometries. When a team of robots moving in a formation, they avoid the obstacle by splitting around

it and rejoining after passing. This approach is scalable to large robot teams since global communication is not used and that local sensing is sufficient to generate effective formation behaviors in large robot teams.

Another method similar to crystal generation which employs a form of probabilistic control is proposed by Fujibayashi et al. [11]. This study makes use of virtual springs to keep two agents in close proximity. Each pair of robots within a certain range of each other, are connected via a virtual spring. Each agent is classified by the number of neighboring agents within this range (number of connections). The robots form triangle lattices that have random outlines. To obtain a desired outline, the virtual springs among some robots are broken with a certain probability. The candidate springs to be broken are chosen depending on the number of connections the robots it join have. This *breaking preference* and the probability of breaking changes from formation to formation. The algorithm uses only local information and is decentralized. One disadvantage of the method is the difficulty of choosing custom parameters for each formation.

A graph-theoretic framework is proposed by Desai [10] for the control of a team of robots moving in an area with obstacles while maintaining a specific formation. The method uses control graphs to define behaviors of robots in the formation. This framework can handle transitions between formations, i.e. between control graphs. Proofs of the mathematical results required to enumerate and classify control graphs are given. Although the computations for control graphs increase with the number of robots, the fact that these computations are decentralized allows the methods described to be scalable to large groups.

Another graph-based approach to *moving in formation* problem is introduced by Fierro and Das [17]. They proposed a four-layer modular architecture for formation control. Group control layer is the highest layer generating a desired trajectory for the whole group to move. Formation control layer implements a physical network, a communication network, and a computational network (control graph). It maintains the formation by using local communication and relative position information. Kinematics control layer deals with the required linear and angular velocities of robots. Finally, the dynamic control layer handles the task of realizing the necessary speeds given by the kinematics control layer. This four-layer architecture provides an abstraction among tasks required at different levels. For example, a robot with different mass, inertia, and friction can be used only by

changing the dynamic control layer. Furthermore a modular adaptive controller is described which can manage control of robots with unknown dynamics and learns the robot dynamics on-the field. Hence using a different robot requires no change in the system. The method described is scalable (control algorithms scale linearly) and flexible (it allows various formations). Centralized and decentralized versions of control graph assignment algorithm is also described in the study.

only local communication and sensor information. Obstacle avoidance is also provided in this method. It extends ordinary behavior-based approaches with the application of social roles that represent positions in the formation and with the use of local communication

to improve performance. As new agents join the formation, the shape is *fixed* by local communications and role changes where necessary. The locally communicated information reaches the leader, i.e. the front most robot, which knows the whole shape of the current formation and which decides on the changes necessary. This information is then propagated to the necessary followers, and the formation is updated. There is no need to predefine social roles or positions for robots. Everything is done dynamically as the formation grows. This method supports various formations and also switching between them, therefore it is flexible as well as being scalable and local. Dudenhofer and Jones [5] designed and implemented a tool to model and simulate collective behavior and interactions of a group of thousands of robots. Using this simulation tool, the problem of hazardous material detection by thousands of micro-robots scattered around a region is tackled. Social potential fields are utilized for coordinated group behavior where robots are desired to stay at a specific distance from others to obtain optimum coverage of the area. They are also required to wander in this formation to search other parts. The desired behavior is obtained by using a subsumption architecture. This study also validates the proposed method in cases where it is possible for agents to die and where agents have imperfect sensor readings. The method uses only local information and is scalable to very large groups of robots. Mataric and Fredslund [9] used local information to establish and maintain formations among robots. Each robot has a unique ID and a designated friend robot which it can see through a friend sensor. There is also minimal communication between robots: heartbeat signals (robots broadcast their IDs), swerve signals (changing direction), and formation messages. Each robot can learn the number of robots in formation and the type of formation using broadcasted messages.

For each formation, each robot has a specified angle which determines the angle it should keep between its front direction and the direction of its friend. This angle is calculated locally. The details of this calculation are given in [9]. This study accomplishes the task of establishing and maintaining formations using only local information and minimal communication.

However the possible formations are limited to chain-shaped ones that do not make a backward curve. One of the major reasons why multi-robot systems are preferred over single-robot systems is their robustness in performance. The robustness of multi-robot systems can be improved by incorporating adaptation mechanisms that can respond to continuing changes in the environment as well as in the capabilities of individual robots.

Adaptation in multi-robot systems

In this section we review the studies that used adaptation strategies in controlling multi-robot systems. Specifically we have investigated (1) how learning (life-long adaptation) is used to make multi-robot systems respond to changes in the environment as well as in the capabilities of individual robots, and (2) how evolution is used to generate group behaviors.

In multi-robot systems, adaptation can be achieved at two levels: group level and individual level. We classify the recent studies into these levels and review them in the following subsections

Individual level adaptation

Large state spaces render reinforcement learning models worthless. One solution to this issue is to use many simpler learning modules for various states rather than one complex one. Research by Takayashi [[26]] is one example. A scaled-down version of the robo-soccer challenge serves as the issue examined in his research. It is expected that adversaries would use a variety of strategies, each tailored to its own strengths and weaknesses. Predictors and planners are the two main types of modules. Based on the opponent's past conduct, the predictor can guess what the opponent will do next. The Planner, on the other hand, will create the best possible next step in light of this forecast. Competing prediction algorithms improve accuracy, with only the best prediction module receiving reinforcement. This generates modules tailored to counteract certain enemy strategies. This study applies the concept of ball



chasing against an unpredictable moving opponent. The outcomes are superior than those of studying a single module on its own. Given enough trials, reinforcement learning converges to the best policy, but in practice, this number of trials is typically too big to be practical. To accelerate the learning process, Piao[20] introduces a new reinforcement learning algorithm. Rule learning, reinforcement learning, and action level selection come together to form this technique, which may be thought of as a set of behavioral rules for a given condition. Instances, which are states that have traversed a certain time range, make up the rule base. After each epoch, we use the data we've collected to assign labels to these occurrences. The data from these examples is then used to formulate rules. These guidelines serve as a prohibition against pointless or destructive behavior. Hard-coded rules guide the overarching strategy of robots and are used in action level selection. Together, sensor data and action level are supplied into the reinforcement algorithm to produce state information. The reinforcement learning module then learns to produce actions based on the state that has been generated using sensory data and the action level. To solve the robosoccer challenge, Piao uses this strategy. He claims enhanced performance on learning with several robots over conventional Q learning, but only if only one agent is learning at a time.

Since reinforcement learning was designed to work with isolated entities, it lacks tools to facilitate social behaviour. In his work, Tangamchit[16] addresses this issue. The paper discusses the split between systems that are action-based and task-based. Reactive behaviors are generated by action level systems in order to address issues. However, task-level systems create tasks that are made up of smaller tasks that may be delegated to different agents. Cooperation, according to Tangamchit, is defined as "task level activity" in which robots may share resources and obligations. There are two potential incentive systems to think about: global and local. Each unit's reinforcement in a global rewardscheme is shared among all members of the group. Under contrast, under a local incentive system, the prize is not shared across the group's individuals. Q-learning and Monte Carlo learning are two of the learning algorithms taken into account. When evaluating the worth of each action over all states, Q-learning utilizes cumulative discounted rewards whereas Monte Carlo learning uses averaging. The

episode's reward is the same for every given pair of state actions. This strategy is less efficient because it does not take into account the impact of later acts in an episode that are more likely to result in a positive outcome.

In this research, we focus on a specific subtype of the foraging issue known as puck collecting behavior. Pucks can only be collected and placed in the bin by robots. Except for the action of depositing a puck, all other actions result in a negative reward. There is a puck-free "home" zone, a puck-filled "deposit" zone, and pucks all over the field. This is accomplished with the help of two quite different robots. The first robot has superior mobility and collection capabilities in non-home environments. The second robot can more quickly complete the bin depositation, but can only travel inside its home territory. For the best results, the robots must work together to transport the pucks back to the home area and then deposit them. Learning at the task level is necessary.

The findings show that local incentives or discounted cumulative rewards, like those used in Q learning, are ineffective for teaching cooperation at the task level. Cooperative strategies for this job emerge instead when global incentives are combined with average rewards. To include domain knowledge, reinforcement learning just needs feedback for the applied sequence of actions. This is often implemented via the selection of reward functions. The role of rewards in a foraging activity is discussed by Mataric[14]. Although mathematically straightforward to examine, single objectives create difficulties in learning and development.

It's challenging to transform actions that are conditional or sequential into a single objective function. Instead, subgoals of the agent are described by many goal functions. Estimators of future advancement are another development. These estimators provide an approximate assessment of progress toward a certain objective. Both of these enhancements (proper subgoal design and subgoal progress estimation) significantly boost the topic's use of domain knowledge. Furthermore, they provide far more reinforcement than conventional approaches by rewarding not just the end result but also smaller, more manageable achievements along the way. Robots performing a real-world foraging activity are used to evaluate the effectiveness of the new strategy. Robots

have the job of bringing pucks back and forth from the rink. Robots are also expected to maintain a presence in the house at regular times. To make the robots' state space of the learning issue more comprehensible, we teach them some basic reactive actions. These actions include dropping pucks while at home, avoiding barriers, and retrieving pucks when they are in close proximity to the agent. The ideal strategy is produced by hand and then compared to the experimental results. The results support the usefulness of both intended changes. The study makes a fascinating point about the disruption that agents may produce. The rate of learning and the degree of convergence suffer as the number of learning agents increases.

Cooperation is achieved in Parker's[6] L-ALLIANCE model via the employment of numerous behavior sets and global communications. A observer is assigned to each behavior set. These watchdogs verify the prerequisites for triggering behavior sets and evaluate the agent's and the group's abilities. Parker presents two drives, impatience and acceptance. Both impatience and acceptance reflect a propensity for a robot to take up a duty that was assigned to another robot. The L-ALLIANCE design shifts these intrinsic incentive factors as the learner progresses. Due to the design, robots must constantly update one another on their present status. This design presupposes that a robot is responsible for all potential environmental modifications that emerge from an activity it states. The issue of credit allocation is therefore resolved. The L-ALLIANCE design has the desirable features of dealing with heterogeneous groups and being resilient in the face of failures or shifts in robot capability. In contrast, L-ALLIANCE's assumption-heavy approach to the credit assignment issue necessitates widespread communication.

According to Goldberg et al. [4,] AMM (Augmented Markov Models) are proposed. The added data regarding transitions in AMM make it a superior Markov model. Instead of producing policy, it is meant to learn from environmental statistics. In contrast to HMMs, which assume that the outcomes of a given set of actions are unknown, AMMs assume that all of the action's details are known.

However, unlike traditional Markov models, AMMs are constructed in stages. They can mimic such higher-order transitions in the system with more accuracy thanks to this incremental buildup. Their research integrates AMMs with BBR [2]. Multiple

AMMs, each with a unique time scale, keep an eye on each behavior. This enables the system to react quickly or slowly to changes in its surroundings.

Group level adaptation

By its very nature, reinforcement learning requires a centralized server, making it impractical for use in multi-robot setups. A compromise between centralized and decentralized learning is proposed in Yanli's study[27] on opportunistically cooperative neural learning. When it comes to purely decentralized learning models, each agent maintains its knowledge of the subject to itself. Because of this, the group's performance suffers greatly because of the lack of common experience. By using 'opportunistic' search, Yanli is able to address this issue. The notion of survival of the fittest in genetic algorithms is conceptually comparable to this approach. Low-t networks learn from high-t ones, and vice versa.

Three cases—a centralized one, a distributed one, and an opportunistically dispersed one—are compared in Yanli's study. These hypotheses are tested on a seeking task in which agents are tasked with covering as much ground in a certain area as they can without making too many trips back and forth. Collaboration seems to be the most effective tactic. Each agent plans its next step in advance, and they all take action at once. In addition, agents often discuss future moves with one another. To anticipate the behavior of other agents, each agent uses these plans. These predictions are learning machines. When it is possible to exactly forecast the future activity of other agents, rewards may be determined.

The findings demonstrate that central learning outperforms all other techniques. However, there are a number of issues with fault-tolerance and communication that plague central learning. Both central learning and OCL (opportunistically cooperative learning) perform noticeably better than the distributed-only situation, with OCL coming out on top.

Agah[1] incorporates both personal and social change into his writing. To solve the multi-robot learning challenge, Agah employs a method called Tropism Architecture. As a bridge between perception and behavior, tropism architecture facilitates education. Each tropism is characterized by a predisposition to react to certain stimuli. Learned tropisms (i.e. state-

action-tendency pairings) are stored in the tropism architecture. Agents make choices by applying tropisms to the present situation. Based on the tropism values, a random process decides what steps to take. This architecture employs both supervised and unsupervised learning methods. Every person's own learningScheme incorporates environmental input into its set of tropisms.Changes include introducing a new legitimate action for the present state, raising the tropism value for a reinforced pair, and switching actions when a negative reinforcement or invalid action is detected.

In population learning, we encode each agent's tropism list as a sequence of bits with varying lengths. A genetic algorithm is used to these sequences of binary digits. Each individual's fitness is determined by adding up all of the positive reinforcement it has received during its own process of learning.Even without reinforcementpropagation as in Q-learning, the results show that this dual approach is effective. Behaviours cannot always be established in advance, and sometimes even behaviours need to be taught. The movement of hexapods is one example. Parker[8] investigated how hexapod robots may learn to do a box-pushing activity together. Since a hexapod robot's movement requires more complex procedures than a wheeled robot's, this is his primary challenge. Parker designed CyclicGenetic Algorithms (CGA), which can manage the complex control needs at hand, for this endeavor.The goal of CGAs is to evolve not only basic stimulus-response pairings, but rather a series of activities. CGA encrypts a sequence of activations that the agent must perform repeatedly.The fitness of each chromosome is determined by running a computer simulation in which the chromosome under evaluation is coupled with the optimal solution to the job at hand. The fitness of the chromosome is evaluated according to the collective's level of success. Using a deliberate approach yields positive results.

For robots to work together, they must be able to coordinate their efforts with one another.The earliest forms of cooperation based their interactions on models of peer communication. This may be necessary for an ideal solution, but it will demand more processing power and data transfer capacity as the number of robots in the system grows.While reducing bottlenecks in communication, local communication does not eliminate them entirely. One approach to breaking through the communication

barrier is to use stigmergy. Scalability is achieved by an implicit communication system, which has been seen in social insects. In order to facilitate collaboration between groups of robots, Yamada[28] has developed a functional implementation of an implicit communicationsystem. The difficulty of pushing a box is addressed using this method. An illuminated target indicates success, and it is thought that the robots can sense their own presence, the presence of other robots, and the existence of barriers. In this setup, walls are portrayed as rigid cubes that are ultimately disregarded. In order to address the issue of implicit communication, the writers create fictitious scenarios. Abstrat models of the world's state are calculated based on the data from the sensors and some very rudimentary storage mechanisms (such as counters for certain sensor readings).The robots' behavior is predetermined by a series of rules. Sensor data is used to inform the application of these regulations.

Conclusion

We reviewed the recent studies on the pattern formation and adaptation in multi-robotssystem. The pattern formation studies are classified into two groups. The first groupincludes studies where the coordination is done by a centralized unit that can oversee the whole group and command the individual robots accordingly. The second groupcontains distributed pattern formation methods for achieving the coordination. The studies that used adaptation strategies in controlling multi-robot systems were classifiedinto two levels: group level and individual level.

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